

Name: Solutions

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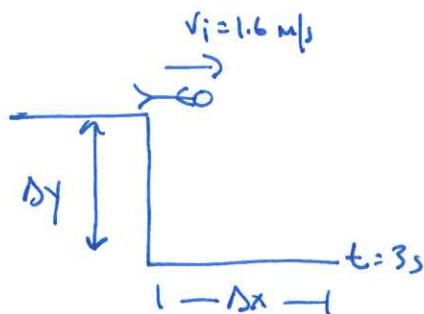
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Accelerated Physics

Mr. Roberts

## Projectile Motion – Case 1 (object launched horizontally) Practice Problems

A diver running 1.6 m/s dives out horizontally from the edge of a vertical cliff and reaches the water below 3 seconds later. How high was the cliff and how far from its base did the diver hit the water?



$$v_{ix} = \frac{\Delta x}{t}$$

$$1.6 = \frac{\Delta x}{3}$$

$$\Delta x = (3)(1.6)$$

$$\Delta x = 4.8 \text{ m}$$

$$\Delta y = v_{iy} t + \frac{1}{2} a_y t^2$$

$$\Delta y = \frac{1}{2} (-9.8) (3)^2$$

$$\Delta y = 44.1 \text{ m}$$

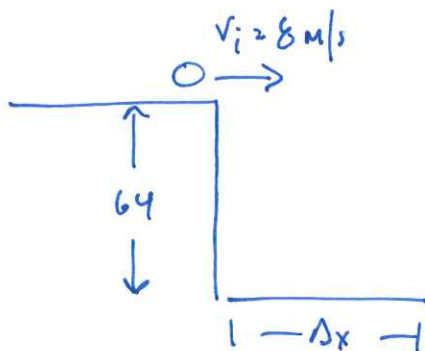
$$v_{ix} = 1.6 \text{ m/s} \quad v_{iy} = 0$$

$$a_x = 0 \quad a_y = -9.8 \text{ m/s}^2$$

$$\Delta x = ? \quad \Delta y = ?$$

$$t = 3$$

1. You accidentally throw your car keys horizontally at 8.0 m/s from a cliff 64 meters high. How far from the base of the cliff should you look for the keys?



Find Time

$$1) \Delta y = v_{iy} t + \frac{1}{2} a_y t^2$$

$$-64 = \frac{1}{2} (-9.8) t^2$$

$$\frac{-128}{-9.8} = t^2$$

$$t = 3.61 \text{ s}$$

2) Find  $\Delta x$

$$v_{ix} = \frac{\Delta x}{t}$$

$$8 = \frac{\Delta x}{3.61}$$

$$\Delta x = 28.91 \text{ m}$$

$$v_{ix} = 8 \text{ m/s} \quad v_{iy} = 0$$

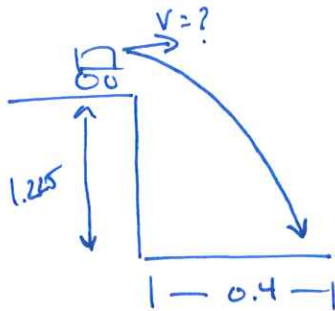
$$\Delta x = ? \quad \Delta y = -64$$

$$a_x = 0 \quad a_y = -9.8$$

$$t = ?$$

2. A toy car runs off the edge of a table that is 1.225 meters high. The car lands 0.400 meters from the base of the table.

- How long did it take the car to fall?
- How fast was the car going on the table before it went off the edge?



$$A) \Delta y = v_{iy} t + \frac{1}{2} a_y t^2$$

$$-1.225 = \frac{1}{2} (-9.8) t^2$$

$$\frac{-2.45}{-9.8} = t^2$$

$$t = 0.5 \text{ s}$$

$$B) v_{ix} = \frac{\Delta x}{t}$$

$$v_{ix} = \frac{0.4}{0.5}$$

$$v_{ix} = 0.8 \text{ m/s}$$

$$\Delta y = -1.225 \quad \Delta x = 0.4$$

$$v_{iy} = 0$$

$$a_y = -9.8$$

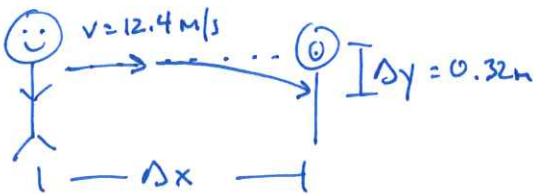
$$v_{ix} = ?$$

$$a_x = 0$$

$$t = ?$$

3. A dart player throws a dart horizontally at 12.4 m/s. The dart hits the board 0.32 m below the height from which it was thrown.

- How long is the dart in the air?
- How far away is the player from the board?



$$v_{ix} = 12.4 \text{ m/s}$$

$$a_x = 0$$

$$\Delta x = ?$$

$$v_{iy} = 0$$

$$a_y = -9.8 \text{ m/s}^2$$

$$\Delta y = -0.32$$

$$t = ?$$

$$A) \Delta y = v_{iy} t + \frac{1}{2} a_y t^2$$

$$-0.32 = \frac{1}{2} (-9.8) t^2$$

$$\frac{-0.64}{-9.8} = t^2$$

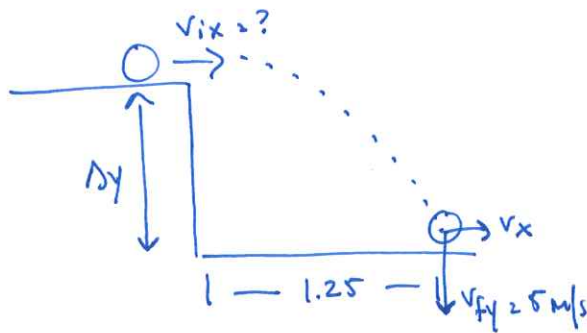
$$t = 0.26 \text{ s}$$

$$B) v_{ix} = \frac{\Delta x}{t}$$

$$12.4 = \frac{\Delta x}{0.26}$$

$$\Delta x = 3.17 \text{ m}$$

4. A ball is rolling towards the edge of a table and falls off. You witness this and observe the ball having a **vertical velocity** of 5 m/s when it hits the floor below 1.25 meters from the base of the table.
- How long did it take the ball to land?
  - How tall is the table?
  - How fast was the ball rolling before it fell off the edge?



$$\begin{aligned} v_{iy} &= 0 & v_{ix} &=? \\ v_{fy} &= -5 \text{ m/s} & \Delta x &= 1.25 \\ \Delta y &=? & a_x &= 0 \\ a_y &= -9.8 \end{aligned}$$

$$t = ?$$

$$\begin{aligned} B) \quad v_{fy}^2 &= v_{iy}^2 + 2 a_y \Delta y \\ (-5)^2 &= 0^2 + 2(-9.8) \Delta y \end{aligned}$$

$$25 = -19.6 \Delta y$$

$$\Delta y = -1.26 \text{ m}$$

or

$$\boxed{1.26 \text{ m tall}}$$

$$\begin{aligned} C) \quad v_{fy} &= v_{iy} + a_y t \\ -5 &= 0 + (-9.8) t \end{aligned}$$

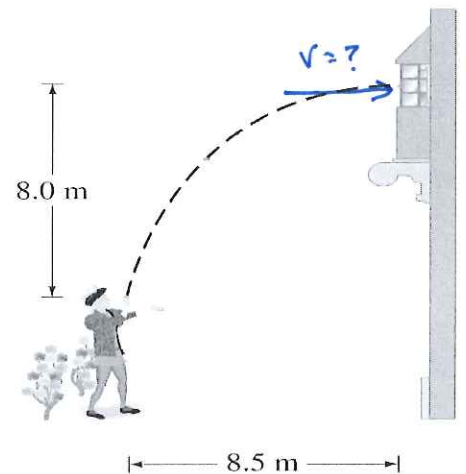
$$\boxed{t = 0.51 \text{ s}}$$

$$A) \quad v_{ix} = \frac{\Delta x}{t}$$

$$v_{ix} = \frac{1.25}{0.51}$$

$$\boxed{v_{ix} = 2.45 \text{ m/s}}$$

5. Romeo is chucking pebbles gently up to Juliet's window, and he wants the pebbles to hit the window with only a horizontal component of velocity. He is standing at the edge of a rose garden 8.0 meters below her window and 8.5 meters from the base of the wall. How fast are the pebbles going when they hit her window?



1) Find time

$$\Delta y = v_{iy} t + \frac{1}{2} a_y t^2$$

$$-8 = \frac{1}{2} (-9.8) t^2$$

$$t = 1.28 \text{ s}$$



Typically down is the negative direction, here we can say up is negative and calculate normally.

$$v_x = \frac{\Delta x}{t}$$

$$v_x = \frac{8.5}{1.28}$$

$$\boxed{v_x = 6.65 \text{ m/s}}$$

$$\Delta y = 8 \text{ m}$$

$$\Delta x = 8.5 \text{ m}$$

$$v_x = ?$$